

לוגיקה – תרגיל 13

הוכיחו את הטענות הבאים:

א.

$$1.(x)(Kx \rightarrow \sim Lx)$$

$$2.(\exists x)(Mx \cdot Lx) \quad / \therefore (\exists x)(Mx \cdot \sim Kx)$$

ב.

$$1.(x)[(Rx \cdot Ax) \rightarrow Tx]$$

$$2.Ab$$

$$3.(x)(Rx) \quad / \therefore Tb$$

ג.

$$1.(x)[(Fx \vee Hx) \rightarrow (Gx \cdot Ax)]$$

$$2.\sim(x)(Ax \cdot Gx) \quad / \therefore (\exists x)\sim Hx$$

$$1.\sim(\exists x)Fx \quad / \therefore Fa \rightarrow Ga \quad \text{ד.}$$

ה.

$$1.(x)[(Ax \cdot Bx) \rightarrow Cx]$$

$$2.Aa \cdot Ba$$

$$3.\sim Cb \quad / \therefore \sim(Ab \cdot Bb)$$

ו.

$$1.(x)(Gx \rightarrow Hx)$$

$$2.(\exists x)(Ix \cdot \sim Hx)$$

$$3.(x)(\sim Fx \vee Gx) \quad / \therefore (\exists x)(Ix \cdot \sim Fx)$$

ז.

$$1.(x)[(Bx \cdot Ax) \rightarrow Dx]$$

$$2.(\exists x)(Qx \cdot Ax)$$

$$3.(x)(\sim Bx \rightarrow \sim Qx) \quad / \therefore (\exists x)(Dx \cdot Qx)$$

ח.

$$1.(x)[Px \rightarrow (Ax \vee Bx)]$$

$$2.(x)[(Bx \vee Cx) \rightarrow Qx] \quad / \therefore (x)[(Px \cdot \sim Ax) \rightarrow Qx]$$

תרגיל אתגר

$$1.(x)[Px \rightarrow (Qx \vee Rx)]$$

$$2.(x)[(Sx \cdot Px) \rightarrow \sim Qx] \quad / \therefore (x)(Sx \rightarrow Px) \rightarrow (x)(Sx \rightarrow Rx)$$

בהצלחה!